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Problem Statement

{ Problem 6.46 in Felder & Rousseau, 2nd Edition }

Similar to Problem 6.60 in F&R, 3rd Ed.

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A saturated-liquid feed mixture containing 30.0 mole% benzene and 70.0 mole% styrene is to be separated in a distillation column. The column produces an overhead product (a saturated-liquid distillate) and a bottoms product. The bottoms product is 99 mole% styrene and contains 2.0% of the benzene fed to the column.

The liquid stream leaving the bottom of the column (not the bottoms product) goes to a partial reboiler, in which a portion of it is vaporized at 150°C and returned to the bottom of the column. The residual liquid from the reboiler is the bottoms product. The vapor and liquid streams exiting the rebolier are in equilibrium. The boilup ratio, or mole ratio of the vapor and liquid streams leaving the reboiler, is 2.5:1.

Calculate the compositions (component mole fractions) of the distillate product, the vapor returned to the column from the reboiler, and the liquid feed to the reboiler, and estimate the required operating pressure of the reboiler. Also, estimate the temperatures of the feed and distillate streams at a pressure of 1 atm.

Conceptual Model $T_{D} = ?$ $P_{D} = 1 \text{ atm}$ $P_{h_{D}} = 1$ $P_{h_{D}} = 1$ $P_{h_{D}} = 1$ $P_{h_{D}} = 1$ E $T_F = ?$ $P_F = 1 \text{ atm}$ $Ph_F = F$ $\dot{N}_F = 1 \text{ or mol/min}$ reflux $X_{P,BZ} = ?$ $T_{y} = T_{B}$ $X_{P,ST} = ?$ column $P_v = P_B$ XF, BZ = 0.300 $Ph_v =$ XFST = 0.700 $\dot{\pi}_{v} = ?$ YU,BZ = ? Yu,ST = ? $\frac{Y_{V,ST} = ?}{F_B} = 150^{\circ}C$ $\frac{150^{\circ}C}{F_B} = ?$ $\frac{B}{PhB} = PhB = ?$ $\frac{B}{PhB} = ?$ $T_{L} = ?$ $P_{L} = ?$ Ph = 119 $\dot{n}_{1} = ?$ XL. BZ = ? XBBZ = 0.0] QR Xhst = ? XB, ST = 0.99 nying = 2.5 boilup ratio other Givens: 0.01 MR = 0.02 (0.30 n=) X_{D,B2} and X_{BST} PB in atm YV;B2 and YV, ST TF in °C XL,B2 and XL, ST TD in °C Finds: XL, BZ and XL, ST © 2007, Michael E. Hanyak, Jr., All Rights Reserved





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Distillation Mathematical Algorithm A [X, TF, TD, MB] = overall [MF, PF, PB, XF] 1. $\dot{n}_{B} \leftarrow 0.02(0.3\dot{n}_{F})/0.01$ 2. $\dot{n}_{D} \leftarrow \dot{n}_{F} - \dot{n}_{B}$ () (1) 2. 3. $\dot{n}_{BBZ} \leftarrow 0.3 \dot{n}_F - 0.01 \dot{n}_B$ 4. $\dot{n}_{BST} \leftarrow 0.7 \dot{n}_F - 0.99 \dot{n}_B$ (<u>)</u> (<u>)</u> 5, XD,BZ ~ np.BZ/Np 6. Xp.ST ~ np.ST/np 6 1) 7. TF & viet [PF, V=0, XF] ③ 8. Tp ← viet [Pp, Vx = 0, Xp] Mathematical Algorithm B [PB, YV, X1] = reboiler [TB, NB, XB] $\dot{n}_{v} \leftarrow 2.5 \dot{n}_{B}$ $\dot{a}_{c} \dot{n}_{L} \leftarrow \dot{n}_{v} + \dot{n}_{B}$ () 3. [PB, YV] < VIEP [TB, Y=0, XB] **S**-D B 4. n, B2 ← n, Yy B2 5. n_{V,ST} ~ n_V Y_{V,ST} 1 6. nL.BZ + NV, BZ + 0.01 nB ٩ 7. nust + nyst + 0.99 mB 3 8. XLBZ ~ MLBZ / ML D 9. XL, ST ~ nL, ST/nL

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Distillation

Numerical Solution A Basis: cgs system, n= 100 mol/min Givens: TR = 150°C $n_B = 0.02(0.3)(100 \frac{mol}{min})/(0.1)$ = [60 mol/min 1. np = (100-60) mol/min 40 mol/min 2. 3. n DBZ = 0.3 (100 min) -0.01 (60 min) = 29.4 mol/min 4. n_Dist = [0.7(100) - 0.99(60)] gmol/min = 10.6 mol/min 5. Xp.BZ = 29.4 min /40 min = {0.74 } XEST = 10.6 mil / 40 mel 6. 0.26 7. $T_F = vlet [latm, V_f = 0, \overline{X}_F] = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$ 8. $T_D = vlet [latm, V_f = 0, \overline{X}_B] = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$ see Page 6 see Page 7 Numerical Solution B 1. ny = 2.5 (60 mol)min) = 150 mol/min 2. n_ = (150 + 60) mol/min = 210 mol/min 3. [PB, YV] = Vlep [150°C, Y = 0, XB] see Page 8 P_B = 899.207 mmHg = Y_{V,ST} = = { Yy, B= = 4. n. = 0.0485 (150 min) = 7,275 mol/min 5. ny ST = 0.9515 (150 min) = 142,725 mol/min 6. n_{LBZ} = 7.275 mol + 0.01 (60 mol) = 7.875 mol/mm 7. nL,57 = 142.725 mol + 0,99(60 mol) = 202.125 mol/min 8. $X_{L,BZ} = 7.875 \frac{mol}{min} / 210 \frac{mol}{min} = 0.0375 = \{0.04\}$ 9. XLET = 202.125 min /210 mol = 0.9625 = {0.96

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Vapor-Liquid Equilibrium Model for the Feed Stream:



// Given Information

Vf = 0.0 P = 760 // mmHG or 1 atm zBZ = 0.30 zST = 1.0 - zBZ

Numerical Solution as given by EZ Setup:

T	kBZ	kST	xBZ	xST	yBZ	yST	zST
<mark>112.241</mark>	2.44796	0.379444	0.3	0.7	0.734389	0.265611	0.7
P 760	Vf 0	zBZ 0.3					

TXY Diagram:



mole fraction of benzene

Vapor-Liquid Equilibrium Model for the Distillate Stream:



// Given Information

Vf = 0.0 P = 760 // mmHG or 1 atm zBZ = 0.735 zST = 1.0 - zBZ

Numerical Solution as given by EZ Setup:

T	kBZ	kST	xBZ	xST	yBZ	yST	zST
<mark>88.8318</mark>	1.30014	0.167549	0.735	0.265	0.9556	0.0444004	0.265
P 760	Vf 0	zBZ 0.735					

TXY Diagram:





Vapor-Liquid Equilibrium Model for the Bottoms Stream:



xBZ + xST - yBZ - yST = 0

// Given Information

Vf = 0.0 T = 150 // C zBZ = 0.01 zST = 1.0 - zBZ

Numerical Solution as given by EZ Setup:

P	PsatBZ	PsatST	kBZ	kST	xBZ	xST	yBZ
<mark>899.207</mark>	4361.18	864.238	4.85003	0.961111	0.01	0.99	<mark>0.0485003</mark>
yST <mark>0.9515</mark>	zST 0.99	T 150	Vf 0	zBZ 0.01			

PXY Diagram:



Heuristic Observation 1. Numerical Solution Model A: $\sum_{i=1}^{2} X_{p_i} = 0.735 + 0.265 = 1.00$ Model B: $\sum_{j=1}^{a} X_{y,j} = 0.0485 + 0.9515 = 1,000$ $\sum_{i=1}^{2} X_{L,i} = 0.0375 + 0.9625 = 1.000$ Check Tr: For pure BZ, THBP = 80,09 °C 7 HYSYS Check Tr For pure ST, THBP = 145.20 °C J 2004 Check To TF = 112° and Tp = 88.8° must be between the normal boiling points of the pure components. for a binary VLE system that is assumed to follow Recult's Law BZ at 150°C, boils at 5.71 atm] HYSYS ST at 150°C, boils at 1, 13 atm J 2004 Check Ps: PB = 1.18 atm must be between these two boilng pressure for the pure components. Also, the VLE system must follow Rooult's Law at 150°C. 2. Math Algorithm What if PB were given and not TB? Then step 3 in Math. Algorithm B would be replaced with [TB, YN] ~ viet [B, Y=0, XB]

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3. Math Mode what if the Raoult's Law assumption did not apply? Then, the following two functional forms would be modelled differently: TT]=Viet[P, 4、三] [P, y] = vlep [T, y, Z] For the PRSV equation of state in HYSYS, you get the following values: Tr = 113.00% °C utt's Tp = 89.33 °C °C Rec Pg = 1.162 atm atm Thus, Raoult's is a good assumption, because the benzene-styrene system behaves like an ideal solution. 4. Conceptual Model What if the boil-up ratio was not given, but reflux ratio was given instead? In the distillation diagram, the reflux ratio 1s: Rp = np/np and the boil-up ratio is: Br = nv/nr Assuming n = n + n and n = n then you can solve the altered problem.

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